## Calibrating a Measuring Device

Name $\qquad$

Partner (s)
Grade /10

## Introduction

The goal of this lab is to understand the need and approach for calibrating an instrument, sensor, or transducer.

## Objectives

By the end of the laboratory exercise, you should have accomplished the following:

- Refreshed knowledge of circuits;
- Reviewed operation and use of basic electronic test equipment;
- Power supply, voltmeter, and bread board.
- Determined calibration constants for an "ohmmeter".


## Equipment Provided

- DC Power supply;
- Fluke Benchtop Digital Multi-Meter (DMM);
- Resistance decade box;
- Breadboard;
- Assorted resistors.


## References

- Instrumentation text book;
- Course web page.


## Procedure - Calibration of an "Ohmmeter"

You are going to be constructing and calibrating a circuit whose purpose is to measure resistance. To do so, you will use a voltage-divider circuit that acts like an ohmeter, and develop a calibration routine to improve the performance of your resistance measuring circuit.

1) Select 3 resistors from the resistor bin: $1 \mathrm{k} \Omega, 10 \mathrm{k} \Omega$, and $100 \mathrm{k} \Omega$. Do not measure their values until the end of this lab.

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2) For the circuit shown at the right, solve analytically for $V_{\text {out }}$ in terms of $V_{i n}, R_{1}$, and $R_{2}$.
3) Now, solve your equation from step 2 for $R_{2}$.

4) The next step is to determine accurate values for $R_{1}$ and $V_{i n}$ in your equation in step 3. You will do this by using optimization techniques applied to data gathered when you measure $V_{\text {out }}$ as a function of $R_{2}$. Wire up the circuit shown above. Use the 3 resistors you selected in step 1 for $\mathrm{R}_{1}$ (one at a time), and use the decade resistance box where $R_{2}$ is indicated in the schematic. Set $V_{\text {in }}$ to $5.00 \mathrm{~V} \pm 1 \%$ and record the actual value below:

$$
\mathrm{V}_{\text {in }}
$$

$\qquad$ VDC
5) Using $R_{1}=1 \mathrm{k} \Omega$, fill in the two columns below with your measured values for $R_{2}$ and $V_{\text {out }}$. Use four significant figures for all measurements.

| $\mathbf{R}_{2}$ <br> Ideal | $\mathbf{R}_{2}$ Measured <br> (resistance box) | Vout |
| :---: | :---: | :---: |
| $0.1 \mathrm{R}_{1}$ |  |  |
| $0.3 \mathrm{R}_{1}$ |  |  |
| $0.5 \mathrm{R}_{1}$ |  |  |
| $0.7 \mathrm{R}_{1}$ |  |  |
| $0.85 \mathrm{R}_{1}$ |  |  |
| $\mathrm{R}_{1}$ |  |  |
| $1.5 \mathrm{R}_{1}$ |  |  |
| $2.5 \mathrm{R}_{1}$ |  |  |
| $4 \mathrm{R}_{1}$ |  |  |
| $7 \mathrm{R}_{1}$ |  |  |
| $10 \mathrm{R}_{1}$ |  |  |

6) Repeat for $R_{1}=10 k \Omega$.

| $\mathbf{R}_{2}$ <br> Ideal | $\mathbf{R}_{2}$ Measured <br> (resistance box | Vout |
| :---: | :---: | :---: |
| $0.1 \mathrm{R}_{1}$ |  |  |
| $0.3 \mathrm{R}_{1}$ |  |  |
| $0.5 \mathrm{R}_{1}$ |  |  |
| $0.7 \mathrm{R}_{1}$ |  |  |
| $0.85 \mathrm{R}_{1}$ |  |  |
| $\mathrm{R}_{1}$ |  |  |
| $1.5 \mathrm{R}_{1}$ |  |  |
| $2.5 \mathrm{R}_{1}$ |  |  |
| $4 \mathrm{R}_{1}$ |  |  |
| $7 \mathrm{R}_{1}$ |  |  |
| $10 \mathrm{R}_{1}$ |  |  |

7) Repeat again for $\mathrm{R}_{1}=100 \mathrm{k} \Omega$.

| $\mathbf{R}_{2}$ <br> Ideal | $\mathbf{R}_{2}$ Measured <br> (resistance box) | Vout |
| :---: | :---: | :---: |
| $0.1 \mathrm{R}_{1}$ |  |  |
| $0.3 \mathrm{R}_{1}$ |  |  |
| $0.5 \mathrm{R}_{1}$ |  |  |
| $0.7 \mathrm{R}_{1}$ |  |  |
| $0.85 \mathrm{R}_{1}$ |  |  |
| $\mathrm{R}_{1}$ |  |  |
| $1.5 \mathrm{R}_{1}$ |  |  |
| $2.5 \mathrm{R}_{1}$ |  |  |
| $4 \mathrm{R}_{1}$ |  |  |
| $7 \mathrm{R}_{1}$ |  |  |
| $10 \mathrm{R}_{1}$ |  |  |

8) Open Excel and load the Solver Add-in by executing the following steps:
a. Go to File $\rightarrow$ Options $\rightarrow$ Addins
b. Select "Solver Add-in" and hit "Go..."
c. Check the Solver Add-In box and hit OK
d. You can now find the Solver entry under the Data tab.
9) Download the Lab2 Excel Solver Spreadsheet file from the course web page. This spread sheet has columns whose purpose is as follows:
a. $\quad \mathbf{R} 2$ Meas - Enter your values of $\mathrm{R}_{2}$ measured from the decade resistance box.

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b. Vout Meas - Enter your measured values of Vout.
c. Vout Calc - These are voltage values calculated using the equation you derived in step 2. Do not modify this column in any way.
d. Sq. Error - The square of the difference between Voutmeas and Voutcalc. These errors are summed in cell D14. Do not modify this column.
e. Vin (Cell E2) - Enter the value of Vin that you measured.
f. $\quad \mathbf{R 1}(\mathrm{Cell} \mathrm{F} 2)$ - Enter the nominal value for $\mathrm{R}_{11}(1000,10000,100000)$.
10) Put your data measurements into the first two Excel columns. Enter 5.000 in cell E 2 (for $\mathrm{V}_{\text {in }}$ measured) and $(1000,10000,100000)$ in cell F2 for the three separate cases of $R_{1}$ measured. Use the Solver function to find the values of $\mathrm{V}_{\text {in }}$ and $\mathrm{R}_{1}$ that minimize the sum-squared error in ( $\mathrm{V}_{\text {outmeas }}$ - $\mathrm{V}_{\text {outcalc }}$ ) while it fits the data to the following equation:

$$
V_{\text {OUT }}=V_{\text {IN }} \frac{R_{2}}{R_{1}+R_{2}}
$$

Record your results from the Solver output:

$$
\begin{array}{lll}
\mathrm{R}_{1}=1 \mathrm{~K} \Omega: & \mathrm{R}_{1 \text { solver }}=\ldots & \mathrm{V}_{\mathrm{IN}, \text { solver }}=\ldots \mathrm{V} \\
\mathrm{R}_{1}=10 \mathrm{~K} \Omega: & \mathrm{R}_{1 \text { solver }}=\ldots & \mathrm{V}_{\mathrm{IN}, \text { solver }}=[\mathrm{V} \\
\mathrm{R}_{1}=100 \mathrm{~K} \Omega: & \mathrm{R}_{1 \text { solver }}=\ldots & \mathrm{V}_{\mathrm{IN}, \text { solver }}=
\end{array}
$$

11) Now measure and record the values of your 3 resistors you selected in step 1 .
$1 \mathrm{k} \ldots \mathrm{k} \Omega \quad 10 \mathrm{k} \ldots \mathrm{k} \Omega \quad 100 \mathrm{k} \quad$ _ $\mathrm{k} \Omega$
12) Use the following formula to calculate percentage errors for measured values vs. solver values for $R_{1}$.

Percentage Error $=\mid($ Measured value - Solver value $) \mid /($ Measured value $) * 100 \%$
1k $\qquad$ \% 10k $\qquad$ \%
100k $\qquad$ \%
13) Next, you are going to compare your calculations using nominal values vs. calibrated values to calculate the value of $\mathrm{R}_{2}$. Use your $\mathrm{R}_{1}=10 \mathrm{~K} \Omega$ resistor for this part. Use the following guide for the table on the following page:

- Second and third column data can be copied from your table in step 6.
- Use your formula derived in step 3 to calculate $\mathrm{R}_{2}$ using Vin $=5.00 \mathrm{~V}$ and $\mathrm{R}_{1}=10 \mathrm{k} \Omega$ (nominal values).
- Use your formula derived in step 3 to calculate $\mathrm{R}_{2}$ using solver values for Vin and $\mathrm{R}_{1}$ (calibrated values).
- Calculate the Per cent Improvement in the last column:

Percent Improvement $=\mid($ Calculated R2 - Calibrated R2) $\mid /($ Calculated R2) $* 100 \%$

| $\mathbf{R}_{2}$ <br> Ideal | $\mathbf{R}_{2}$ Measured <br> (resistance box) | Vout | Calculated R2 | Calibrated R2 | Percent <br> Improvement |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $1 \mathrm{k} \Omega$ |  |  |  |  |  |
| $3 \mathrm{k} \Omega$ |  |  |  |  |  |
| $5 \mathrm{k} \Omega$ |  |  |  |  |  |
| $7 \mathrm{k} \Omega$ |  |  |  |  |  |
| $8.5 \mathrm{k} \Omega$ |  |  |  |  |  |
| $10 \mathrm{k} \Omega$ |  |  |  |  |  |
| $15 \mathrm{k} \Omega$ |  |  |  |  |  |
| $25 \mathrm{k} \Omega$ |  |  |  |  |  |
| $40 \mathrm{k} \Omega$ |  |  |  |  |  |
| $70 \mathrm{k} \Omega$ |  |  |  |  |  |
| $100 \mathrm{k} \Omega$ |  |  |  |  |  |

Draw conclusions regarding any improvement in calculating the value of $\mathrm{R}_{2}$ using nominal vs. calibrated values.

## Summary

What you have done in this lab is find accurate values for the internal characteristics of the meter you created to measure resistance. This is precisely what calibration does - attempts to get an accurate handle on how an instrument or sensor can be mathematically modelled to provide the most accurate results in spite of internal variations between instruments.

